NAME

Module 11Transformations of ShapesLesson 3Dilations

Lesson Notes 11.3

Lesson Objectives

- Draw and describe dilations (enlargements and reductions) of two-dimensional figures.
- Graph dilations on a coordinate plane.

Subtopic 1

Dilations

Dilation

- Figure changes <u>size</u> but not shape.
- Figure and its image are **similar**.
- An <u>enlargement</u> if the image is larger than the original figure
- A <u>reduction</u> if the image is smaller than the original figure

Scale factor

- A number that indicates how much larger—or smaller—the image is from the original
- Describes the size of the change from the original figure to its image

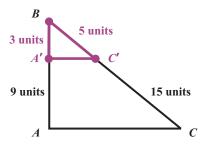
Enlargement

- A dilation with scale factor ≥ 1
- The image is larger than the figure.

Reduction

- A dilation with $0 < \underline{scale factor} < 1$
- The image is smaller than the figure.

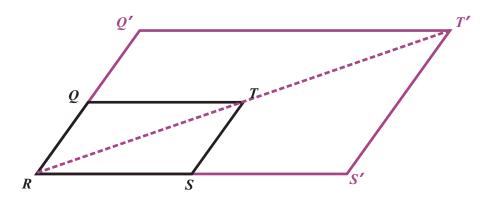
In a dilation with scale factor = 1, the figure and its image have the <u>same</u> points. The <u>center</u> of dilation is a fixed point from which all points contract or expand to make the similar image. Construct a dilation on $\triangle ABC$ with scale factor $\frac{1}{3}$ and center *B*.





1

Construct a dilation of quadrilateral QRST with scale factor two and center R.





3

Dilations on the Coordinate Plane

 Δ *FGH* has vertices *F* (2, 8), *G* (0, -4), and *H* (-3, 5). What are the vertices of an image with a (0,0) center and a scale factor of 5?

$$\begin{array}{rcl} F(2,8) & \rightarrow & F'(2 \times 5,8 \times 5) \rightarrow & F'(10,40) \\ G(0,-4) & \rightarrow & G'(0 \times 5,-4 \times 5) \rightarrow & G'(0,-20) \\ H(-3,5) & \rightarrow & H'(-3 \times 5,5 \times 5) \rightarrow & H'(-15,25) \end{array}$$

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Quadrilateral *PRST* is the image of quadrilateral *VWXY* under a dilation with center (0, 0). What is the scale factor of the dilation?

$$V(-6, -3) \rightarrow P(-2, -1)$$

$$W(0, -6) \rightarrow R(0, -2)$$

$$X(3, 3) \rightarrow S(1, 1)$$

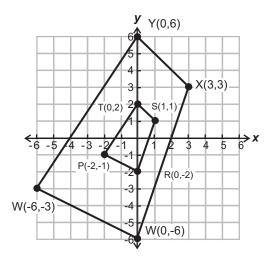
$$Y(0, 6) \rightarrow T(0, 2)$$

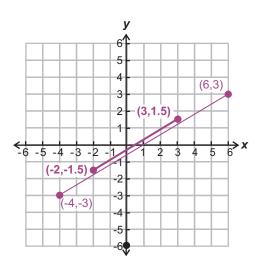
Scale factor: $\frac{1}{3}$



Graph the image of a line segment with endpoints at (-4, -3) and (6, 3) under a dilation with scale factor $\frac{1}{2}$.

$$\left(6 \times \frac{1}{2}, 3 \times \frac{1}{2}\right) \rightarrow \left(3, 1\frac{1}{2}\right) = (3, 1.5)$$
$$\left(-4 \times \frac{1}{2}, -3 \times \frac{1}{2}\right) \rightarrow \left(-2, -1\frac{1}{2}\right) = (-2, -1.5)$$







Graph the image of $\triangle BCD$ under a dilation with scale factor 2.

 $B'(0 \times 2, 2 \times 2) \rightarrow (0, 4)$ $C'(2 \times 2, -3 \times 2) \rightarrow (4, -6)$ $D'(-2 \times 2, -1 \times 2) \rightarrow (-4, -2)$

